Generalizing Lenses

Daniel Wagner

August 19, 2013





Traditional lenses

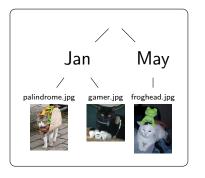
Symmetry

Edits

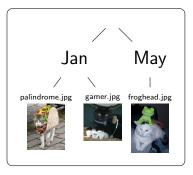
Multidirectionality

Logistics

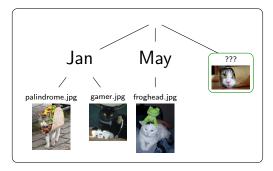
Traditional lenses









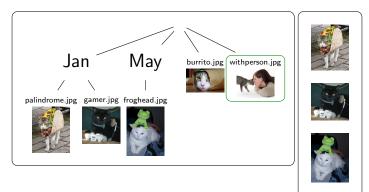




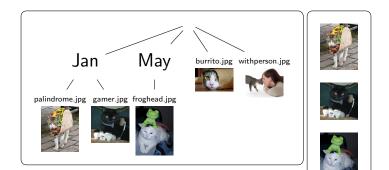
















A lens $\ell \in X \stackrel{a}{\leftrightarrow} Y$ has components

$$get \in X \to Y$$
$$put \in Y \times X \to X$$

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Synchronizing too often doesn't hurt.

$$get(put(y, x)) = y$$

 $put(get(x), x) = x$

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$$put(y', put(y, x)) = put(y', x)$$

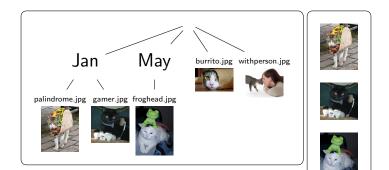
Not synchronizing often enough doesn't hurt.

Related work: asymmetric lenses

- Combinators for Bidirectional Tree Transformations (Foster, Greenwald, Moore, Pierce, Schmitt; POPL 2005)
- Relational Lenses: A Language For Updateable Views (Bohannon, Vaughn, and Pierce; PODS 2006)
- Boomerang: Resourceful Lenses for String Data (Bohannon, Foster, Pierce, Pilkiewicz, and Schmitt; POPL 2008)
- Bidirectional Programming Languages (Foster; thesis 2009)
- Bidirectionalizing Graph Transformations (Hidaka, Hu, Inaba, and Kato; ICFP 2010)
- Update Semantics of Relational Views (Bancilhon and Spyratos; 1981)

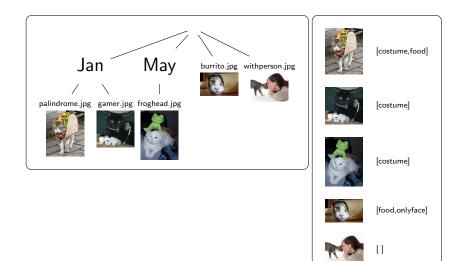
Symmetry

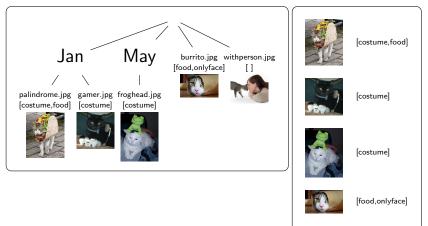
(in collaboration with Martin Hofmann and Benjamin Pierce)





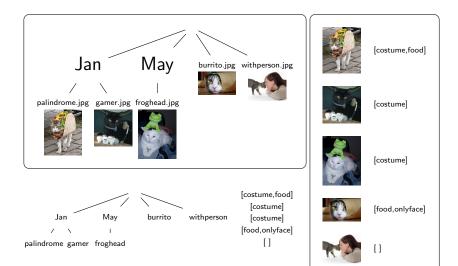


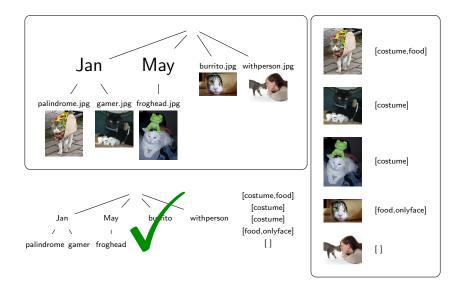












A lens $\ell \in X \stackrel{s}{\leftrightarrow} Y$ has a set *C* and components

$$putr \in X \times C \rightarrow Y \times C$$
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Twist: equational reasoning

$$\mathsf{A} \xleftarrow[k]{a} \mathsf{B} \xleftarrow[\ell]{a} \mathsf{C} \xleftarrow[m]{a} \mathsf{D}$$

Nice property of asymmetric lenses:

$$(k; \ell); m = k; (\ell; m)$$

Twist: equational reasoning

$$\mathsf{A} \xleftarrow[k]{a} \mathsf{B} \xleftarrow[\ell]{a} \mathsf{C} \xleftarrow[m]{a} \mathsf{D}$$

Nice property of asymmetric lenses:

$$(k; \ell); m = k; (\ell; m)$$

Not true for symmetric lenses!

In dissertation

- Observational equivalence
- Point-free programming language
 - Basic (non-recursive) data types
 - Lists, with folds and unfolds
 - Some generalized container operations
- Proof that this generalizes asymmetric lenses

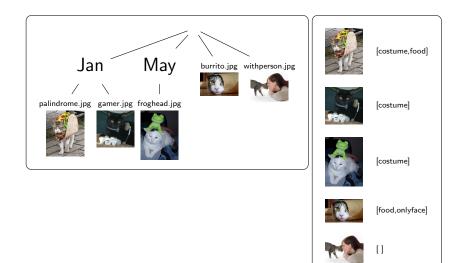
Related work: other symmetric approaches

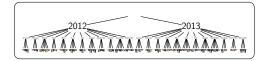
- Symmetric Constraint Maintainers (Meertens; 1998)
- Towards an Algebraic Theory of Bidirectional Transformations (Stevens; ICGT 2008)
- Bidirectional Model Transformations in QVT: Semantic Issues and Open Questions (Stevens; MoDELS 2007)
- Algebraic Models for Bidirectional Model Synchronization (Diskin; MoDELS 2008)
- Supporting Parallel Updates with Bidirectional Model Transformations

(Xiong, Song, Hu, and Takeichi; ICMT 2009)

Edits

(in collaboration with Martin Hofmann and Benjamin Pierce)





Abstract model Edit lens $\ell \in (M, X, \cdot) \stackrel{\delta}{\leftrightarrow} (N, Y, \odot)$ has set C and

$dputr \in M \times C \rightarrow N \times C$ $dputl \in N \times C \rightarrow M \times C$

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$$dputr(m, c) = (n, c')$$
$$dputr(m', c') = (n', c'')$$
$$dputr(mm', c) = (nn', c'')$$

Notable benefits

- All changes reported, so synchronizing less often is less controversial
- Intentional information in edits aids alignment
- Smaller complement in many cases!
- Roundtrip laws are monoid homomorphism laws

Notable benefits

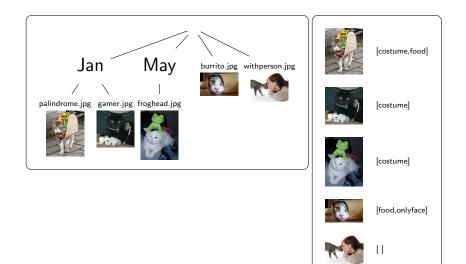
- All changes reported, so synchronizing less often is less controversial
- Intentional information in edits aids alignment
- Smaller complement in many cases!
- Roundtrip laws are monoid homomorphism laws
- Observational equivalence, combinator language, generalizes symmetric lenses

Related work: other edit-based approaches

- Towards an Algebraic Theory of Bidirectional Transformations (Stevens; ICGT 2008)
- Matching Lenses: Alignment and View Update (Barbosa, Cretin, Foster, Greenberg, and Pierce; ICFP 2010)
- From State- to Delta-based Bidirectional Model Transformations (Diskin, Xiong, Czarnecki; TPMT 2010)
- From State- to Delta-based Bidirectional Model Transformations: The Symmetric Case (Diskin, Xiong, Czarnecki, Ehrig, Hermann, and Orejas; MoDELS 2011)
- Delta Lenses over Inductive Types (Pacheco, Cunha, Hu; ECEASST 2012)

Multidirectionality

(in collaboration with Jen Paykin, Benjamin Pierce, Jeff Vaughan, and Geoff Washburn)





[costume,food]



[costume]



[costume]



[food,onlyface]



[]













food



onlyface

| | A | В | С | D |
|---|-------|----------|-----------|--------|
| 1 | | Students | Equipment | Total |
| 2 | 2012 | 70000 | 9000 | 79000 |
| 3 | 2013 | 70000 | 4000 | 74000 |
| 4 | Total | 140000 | 13000 | 153000 |

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|-------|----------|-----------|--------|
| 2012 | 70000 | 9000 | 79000 |
| 2013 | 70000 | 4000 | 74000 |
| Total | 140000 | 26000 | 166000 |

| | Students | Equipment | Total |
|-------|----------|-----------|--------|
| 2012 | 70000 | 18000 | 79000 |
| 2013 | 70000 | 8000 | 74000 |
| Total | 140000 | 26000 | 166000 |

| | Students | Equipment | Total |
|-------|----------|-----------|--------|
| 2012 | 70000 | 18000 | 88000 |
| 2013 | 70000 | 8000 | 78000 |
| Total | 140000 | 26000 | 166000 |

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... and this happens behind the scenes, too.

Straw-man abstract model

For universe U, lens $\ell \in \mathcal{M}(N)$ has components

$$put \in 2^N \to U^N \to U^N$$

 $K \in 2^{U^N}$

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Inputs are really inputs and consistency is restored.

$$put(S,f)|_S = f|_S$$
 $put(S,f) \in K$

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Inputs are really inputs and consistency is restored.

$$put(S, f)|_{S} = f|_{S}$$

 $put(S, f) \in K$
 $put(\emptyset, f) = f$

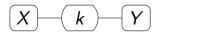
Synchronizing too often doesn't hurt.

Unsolvable updates

StudentsEquipmentTotal201270000900079000201370000400074000Total001

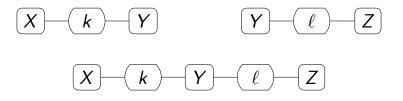
Track sets of names that are always solvable.

Composition intuition

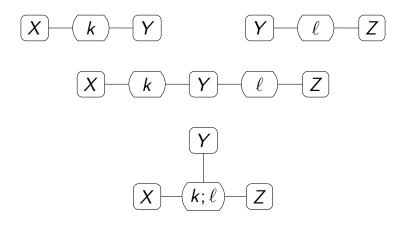




Composition intuition

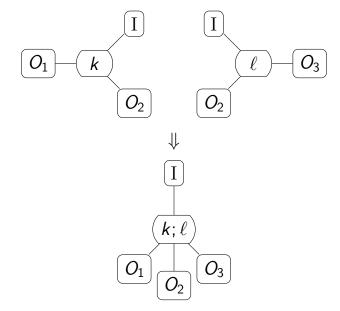


Composition intuition

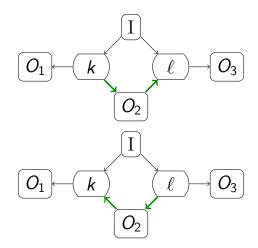


Safe updates: $\{X\}$ or $\{Z\}$.

Ambiguous updates







Observational equivalence is no help.

Remaining questions

- Complete strategies for disambiguation?
- Behavioral specifications for disambiguation?
- How can we extend the static update check?
- What dynamic update checks are possible?

Related work: bidirectional spreadsheets

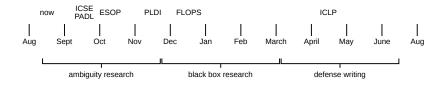
- Tiresias: The Database Oracle for How-To Queries (Meliou and Suciu; SIGMOD ICMD 2012)
- A Spreadsheet Based on Constraints (Stadelmann; UIST 1993)
- SkyBlue: A Multi-way Local Propagation Constraint Solver for User Interface Construction (Sannella; UIST 1994)
- Expressing Multi-way Dataflow Constraint Systems as a Commutative Monoid Makes Many of their Properties Obvious (Järvi, Haveraaen, Freeman, and Marcus; SIGPLAN WGP 2012)
- A Constraint-Based Spreadsheet for Cooperative Production Planning

(Chew and David; KBPPSC 1992)

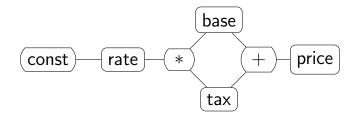
- How to Use the Spreadsheet Manager (Evans; tech report 1993)
- Interval Constraint Spreadsheets for Financial Planning (Hyvőnen; AIAWS 1991)

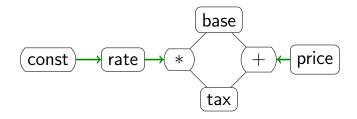
Logistics

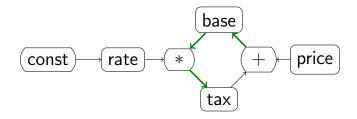
Timeline

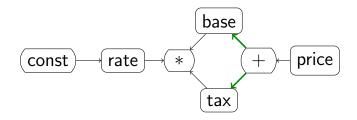


- Nailing ambiguity resolution is lynchpin
- Extending static and dynamic checks is polish
- Bad case: trade black box time for additional ambiguity time
- Worst case: biased composition

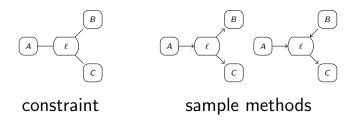








How to progress



- When any plan will do: greedy algorithm
- Assign a cost to each method
- Specification: min-cost set of methods
- Implementation: search (efficient when combining costs is monotonic)