# Generalizing Lenses 

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## Thesis Proposal

There are many fundamentally bidirectional settings that call for generalizations of traditional lenses where a language is possible and helpful.

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## Overview

Traditional lenses

Symmetry

Edits

Multidirectionality

Logistics

## Traditional lenses







## Abstract model

A lens $\ell \in X \stackrel{a}{\leftrightarrow} Y$ has components

$$
\begin{aligned}
& \text { get } \in X \rightarrow Y \\
& \text { put } \in Y \times X \rightarrow X
\end{aligned}
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Synchronizing too often doesn't hurt.

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\begin{aligned}
& \operatorname{get}(\operatorname{put}(y, x))=y \\
& \operatorname{put}(\operatorname{get}(x), x)=x
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\begin{aligned}
\operatorname{get}(\operatorname{put}(y, x)) & =y \\
\operatorname{put}(\operatorname{get}(x), x) & =x \\
\operatorname{put}\left(y^{\prime}, \operatorname{put}(y, x)\right) & =\operatorname{put}\left(y^{\prime}, x\right)
\end{aligned}
$$

Not synchronizing often enough doesn't hurt.

## Related work: asymmetric lenses

- Combinators for Bidirectional Tree Transformations
(Foster, Greenwald, Moore, Pierce, Schmitt; POPL 2005)
- Relational Lenses: A Language For Updateable Views
(Bohannon, Vaughn, and Pierce; PODS 2006)
- Boomerang: Resourceful Lenses for String Data
(Bohannon, Foster, Pierce, Pilkiewicz, and Schmitt; POPL 2008)
- Bidirectional Programming Languages
(Foster; thesis 2009)
- Bidirectionalizing Graph Transformations
(Hidaka, Hu, Inaba, and Kato; ICFP 2010)
- Update Semantics of Relational Views
(Bancilhon and Spyratos; 1981)


## Symmetry

(in collaboration with Martin Hofmann and Benjamin Pierce)







## Abstract model

A lens $\ell \in X \stackrel{s}{\leftrightarrow} Y$ has a set $C$ and components

$$
\begin{aligned}
& \text { putr } \in X \times C \rightarrow Y \times C \\
& \text { putl } \in Y \times C \rightarrow X \times C
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\frac{\operatorname{putr}(x, c)=\left(y, c^{\prime}\right)}{\operatorname{put}\left(y, c^{\prime}\right)=\left(x, c^{\prime}\right)}
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\operatorname{putr}(x, c)=\operatorname{putr}\left(x, c^{\prime}\right)
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## Twist: equational reasoning

$$
\mathrm{A} \underset{k}{\stackrel{a}{\longleftrightarrow}} \mathrm{~B} \underset{\ell}{\stackrel{a}{\leftrightarrows}} \mathrm{C} \underset{m}{\stackrel{a}{\leftrightarrows}} \mathrm{D}
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Nice property of asymmetric lenses:

$$
(k ; \ell) ; m=k ;(\ell ; m)
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Nice property of asymmetric lenses:

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Not true for symmetric lenses!

## In dissertation

- Observational equivalence
- Point-free programming language
- Basic (non-recursive) data types
- Lists, with folds and unfolds
- Some generalized container operations
- Proof that this generalizes asymmetric lenses


## Related work: other symmetric approaches

- Symmetric Constraint Maintainers
(Meertens; 1998)
- Towards an Algebraic Theory of Bidirectional Transformations
(Stevens; ICGT 2008)
- Bidirectional Model Transformations in QVT: Semantic Issues and Open Questions
(Stevens; MoDELS 2007)
- Algebraic Models for Bidirectional Model Synchronization
(Diskin; MoDELS 2008)
- Supporting Parallel Updates with Bidirectional Model Transformations
(Xiong, Song, Hu, and Takeichi; ICMT 2009)


## Edits

(in collaboration with Martin Hofmann and Benjamin Pierce)



## Abstract model

Edit lens $\ell \in(M, X, \cdot) \stackrel{\delta}{\leftrightarrow}(N, Y, \odot)$ has set $C$ and

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& \text { dputr } \in M \times C \rightarrow N \times C \\
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\begin{aligned}
\operatorname{dputr}(m, c) & =\left(n, c^{\prime}\right) \\
\operatorname{dputr}\left(m^{\prime}, c^{\prime}\right) & =\left(n^{\prime}, c^{\prime \prime}\right) \\
\operatorname{dputr}\left(m m^{\prime}, c\right) & =\left(n n^{\prime}, c^{\prime \prime}\right)
\end{aligned}
$$

## Notable benefits

- All changes reported, so synchronizing less often is less controversial
- Intentional information in edits aids alignment
- Smaller complement in many cases!
- Roundtrip laws are monoid homomorphism laws


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- All changes reported, so synchronizing less often is less controversial
- Intentional information in edits aids alignment
- Smaller complement in many cases!
- Roundtrip laws are monoid homomorphism laws
- Observational equivalence, combinator language, generalizes symmetric lenses


## Related work: other edit-based approaches

- Towards an Algebraic Theory of Bidirectional Transformations
(Stevens; ICGT 2008)
- Matching Lenses: Alignment and View Update (Barbosa, Cretin, Foster, Greenberg, and Pierce; ICFP 2010)
- From State- to Delta-based Bidirectional Model Transformations
(Diskin, Xiong, Czarnecki; TPMT 2010)
- From State- to Delta-based Bidirectional Model Transformations: The Symmetric Case
(Diskin, Xiong, Czarnecki, Ehrig, Hermann, and Orejas; MoDELS 2011)
- Delta Lenses over Inductive Types
(Pacheco, Cunha, Hu; ECEASST 2012)


## Multidirectionality

(in collaboration with Jen Paykin, Benjamin Pierce, Jeff Vaughan, and Geoff Washburn)



|  |  | B | c | D |
| :---: | :---: | :---: | :---: | :---: |
| 1 |  | Students | Equipment | Total |
| 2 | 2012 | 70000 | 9000 | 79000 |
| 3 | 2013 | 70000 | 4000 | 74000 |
| 4 | Total | 140000 | 13000 | 153000 |

## New interaction mode

Students Equipment Total<br>201270000900079000<br>201370000400074000<br>Total 14000013000153000

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## New interaction mode

|  | Students | Equipment | Total |
| :--- | :---: | :---: | :---: |
| 2012 | 70000 | 18000 | 88000 |
| 2013 | 70000 | 8000 | 78000 |
| Total | 140000 | 26000 | 166000 |

... and this happens behind the scenes, too.

## Straw-man abstract model

For universe $U$, lens $\ell \in \mathcal{M}(N)$ has components

$$
\begin{aligned}
& \text { put } \in 2^{N} \rightarrow U^{N} \rightarrow U^{N} \\
& K \in 2^{U^{N}}
\end{aligned}
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Inputs are really inputs and consistency is restored.

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\left.\operatorname{put}(S, f)\right|_{S} & =\left.f\right|_{S} \\
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$$
\begin{aligned}
\left.\operatorname{put}(S, f)\right|_{S} & =\left.f\right|_{S} \\
\operatorname{put}(S, f) & \in K \\
\operatorname{put}(\emptyset, f) & =f
\end{aligned}
$$

Synchronizing too often doesn't hurt.

## Unsolvable updates

|  | Students | Equipment | Total |
| :---: | :---: | :---: | :---: |
| 2012 | 70000 | 9000 | 79000 |
| 2013 | 70000 | 4000 | 74000 |
| Total | 0 | 0 | 1 |

Track sets of names that are always solvable.

## Composition intuition



## Composition intuition

$$
\begin{gathered}
X-k-Y \quad Y-(Z-Z \\
X-k-Y-Z-Z
\end{gathered}
$$

## Composition intuition



Safe updates: $\{X\}$ or $\{Z\}$.

## Ambiguous updates



## Two plans



Observational equivalence is no help.

## Remaining questions

- Complete strategies for disambiguation?
- Behavioral specifications for disambiguation?
- How can we extend the static update check?
- What dynamic update checks are possible?


## Related work: bidirectional spreadsheets

- Tiresias: The Database Oracle for How-To Queries (Meliou and Suciu; SIGMOD ICMD 2012)
- A Spreadsheet Based on Constraints
(Stadelmann; UIST 1993)
- SkyBlue: A Multi-way Local Propagation Constraint Solver for User Interface Construction
(Sannella; UIST 1994)
- Expressing Multi-way Dataflow Constraint Systems as a Commutative Monoid Makes Many of their Properties Obvious
(Järvi, Haveraaen, Freeman, and Marcus; SIGPLAN WGP 2012)
- A Constraint-Based Spreadsheet for Cooperative Production Planning
(Chew and David; KBPPSC 1992)
- How to Use the Spreadsheet Manager
(Evans; tech report 1993)
- Interval Constraint Spreadsheets for Financial Planning
(Hyvőnen; AIAWS 1991)


## Logistics

## Timeline



- Nailing ambiguity resolution is lynchpin
- Extending static and dynamic checks is polish
- Bad case: trade black box time for additional ambiguity time
- Worst case: biased composition


## Why black boxes?

$$
\begin{aligned}
\text { price } & =\text { base }+ \text { tax } \\
\text { tax } & =0.08 * \text { base }
\end{aligned}
$$



## Why black boxes?

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## How to progress


constraint

sample methods

- When any plan will do: greedy algorithm
- Assign a cost to each method
- Specification: min-cost set of methods
- Implementation: search (efficient when combining costs is monotonic)

